# Study Guide for 2019 QR exam Numerical Linear Algebra (Math 5165) 

[ Reference: Numerical Liner Algebra, SIAM 1997, Author: L. Trefethen and D. Bau, III]

1: ... (i) Singular Value Decomposition
(ii) LU factorization, and Cholesky factorization
(iii) Steepest descent
(iv) Conjugate Gradient method

Example:

$$
A=\left[\begin{array}{lll}
1 & 2 & 3 \\
4 & 5 & 6 \\
7 & 8 & 9
\end{array}\right] \quad b=\left[\begin{array}{l}
2 \\
5 \\
8
\end{array}\right], X=[x, y, z]^{T}
$$

(1) Find the singular value decomposition of $A$ (2) Use Cholesky factorization to solve $A A^{T} X=b$. (3) Use LU factorization to solve $A X=b$ (4) Use Conjugate gradient to solve $A A^{T} X=b$.

2: Part I: Lectures 1-5 (Fundamentals)
3: Part II: Lectures 6,7,8, 10, 11(QR factorization and Least Squares)
4: Part IV: Lectures 20, 21, 22, 23 (Direct Methods)
5: Part VI: Lectures 32 33, 35, 38 (Iterative Methods)

