Math 8276: Qualifying Exam Syllabus

August 2023 Exam

Textbooks:

- Introduction to Dynamical Systems, by Michael Brin and Garrett Stuck
- An Introduction to Ergodic Theory, by Peter Walters
- Equilibrium States and the Ergodic Theory of Anosov Diffeomorphisms, by Rufus Bowen

Ergodic theory

- Recurrence
- Ergodicity and mixing
- Examples
- Ergodic theorems
- Invariant measures for continuous maps

Entropy theory

- Entropy of a partition
- Conditional entropy
- Entropy of a measure-preserving transformation
- Examples
- Variational principle

Thermodynamic formalism

- Gibbs measures
- Ruelle's Perron-Frobenius Theorem
- Construction of Gibbs measures
- Variational principle
- Further properties