

1. Find the domain of the function  $f(x) = \frac{\sqrt{x+2}}{x}$ .

- a.  $(-\infty, -2]$
- b.  $[-2, \infty)$
- c.  $[-2, 0) \cup (0, \infty)$
- d.  $[-\infty, 0) \cup (0, \infty)$
- e.  $[-2, 0)$

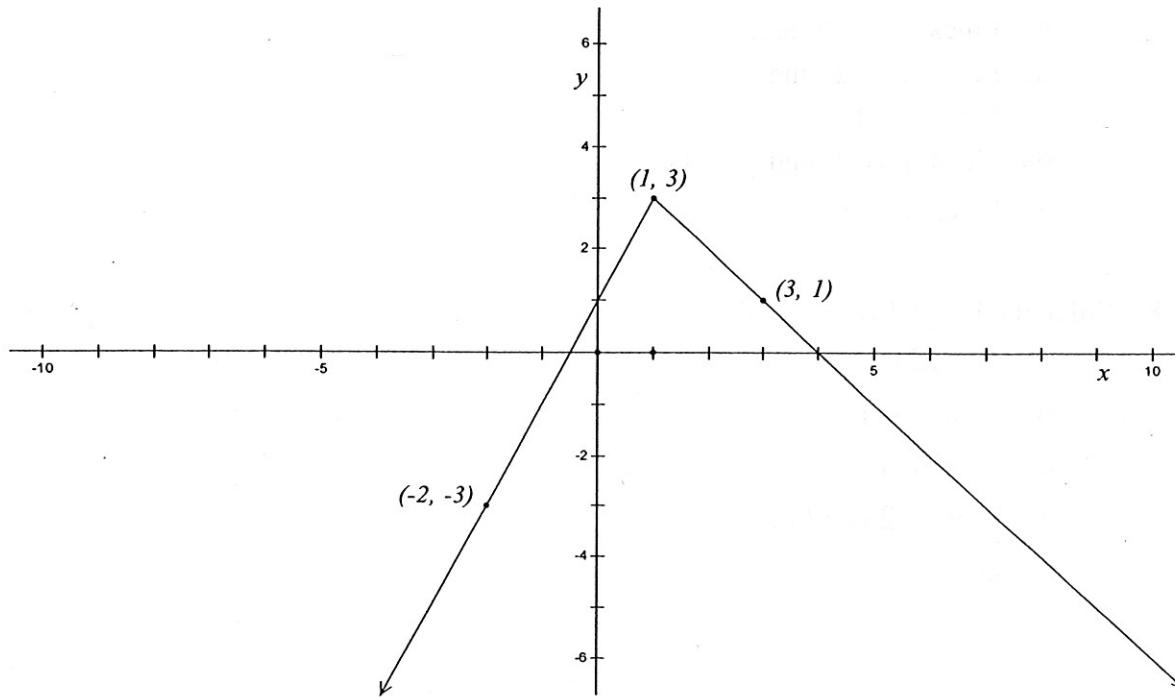
2. If you shift the graph of  $y = f(x)$  four units down and two units to the left, you get the graph

- a.  $y = f(x+2)+4$
- b.  $y = f(x-2)+4$
- c.  $y = f(x-4)+2$
- d.  $y = f(x+4)-2$
- e.  $y = f(x+2)-4$

3. Choose the piecewise function for the given graph.

- a.  $\begin{cases} 3, & \text{for } x > 1 \\ -1, & \text{for } x < 1 \end{cases}$
- b.  $\begin{cases} x-1, & \text{for } x \leq 1 \\ -x, & \text{for } x \geq 1 \end{cases}$
- c.  $\begin{cases} 2x-2, & \text{for } x < 1 \\ -x-2, & \text{for } x \geq 1 \end{cases}$

- d.  $\begin{cases} x+2, & \text{for } x < 1 \\ 2-x, & \text{for } x > 1 \end{cases}$
- e.  $\begin{cases} 2x+1, & \text{for } x \leq 1 \\ 4-x, & \text{for } x > 1 \end{cases}$



4. Let  $f(x) = x - 2$ , find  $f(f(f(f(5))))$ .

- a. 5
- b. 3
- c. 1
- d. -1
- e. -3

5. If the point  $(2, -1)$  is on the graph of  $f(x)$  and  $f(x)$  is known to be odd, what other point must be on the graph of  $f(x)$ ?

- a.  $(2, -1)$
- b.  $(-2, -1)$
- c.  $(-2, 1)$
- d.  $(2, 1)$
- e.  $(-1, 2)$

6. Find the domain (D) and range (R) of the function  $f(x) = 19x^2 - 19$ .

- a.  $D = (-1, 1), R = (0, \infty)$
- b.  $D = (-\infty, \infty), R = (0, \infty)$
- c.  $D = (-1, 1), R = (19, \infty)$
- d.  $D = (-\infty, \infty), R = [19, \infty)$
- e.  $D = (-\infty, \infty), R = [-19, \infty)$

7. Find the vertical asymptotes (VA) of  $f(x) = \frac{x^2 - 9}{x^2 - 5x + 6}$ .

- a. Lines  $x = -2$  and  $x = -3$
- b. Lines  $x = 2$  and  $x = 3$
- c. Line  $x = 2$
- d. Lines  $y = 2$  and  $y = 3$
- e. Lines  $y = 1$

8. Solve the inequality  $x^2 > 4$ .

- a.  $(-2, 2)$
- b.  $(-2, -\infty)$
- c.  $(-4, \infty)$
- d.  $(-\infty, -2) \cup (2, \infty)$
- e.  $(0, \infty)$

9. Let  $f(x) = \frac{x+2}{x-3}$ . Find  $f^{-1}(-1)$ .

- a.  $\frac{1}{2}$
- b.  $-\frac{1}{2}$
- c. 3
- d.  $-\frac{5}{2}$
- e. undefined

10. Let  $f(x) = \frac{1}{x}$ . Find  $\frac{f(x+h)-f(x)}{h}$ .

- a.  $f(x) = \frac{h}{x(x+h)}$
- b.  $f(x) = \frac{1}{x^2}$
- c.  $f(x) = \frac{-1}{x(x+h)}$
- d.  $f(x) = \frac{2x-h}{x(x+h)h}$
- e.  $f(x) = \frac{1}{x(x+h)}$

11. Which of the following numbers is *not* a potential rational zero of the polynomial function  $f(x) = 2x^3 + x^2 + 36$ .

- a.  $\frac{-1}{2}$
- b.  $\frac{-3}{2}$
- c.  $\frac{1}{3}$
- d. 12
- e. 4

12. Given the equation  $3^x = e^{x+1}$ , solve for  $x$  and approximate its value to four decimal places.

- a. -10.1407
- b. 10.1407
- c. -0.0986
- d. 0.0986
- e. -10.1479

13. Rewrite  $\ln(1000^x)$  in terms of  $\ln(5)$  and  $\ln(2)$ .

- (a)  $x(3 \ln(5) + 3 \ln(2))$
- (b)  $9 \ln(5) \ln(2)$
- (c)  $3x^2 \ln(5) \ln(2)$
- (d)  $3x \ln(5) - 4x \ln(2)$
- (e)  $x(2 \ln(5) + 4 \ln(2))$

14. Solve for  $x$  in the following equation  $1 + \log(7) = 2x + 3x \log(7)$ .

- a.  $\frac{1}{2 + 3 \log(7)}$
- b.  $\frac{2 + 3 \log(7)}{1 + \log(7)}$
- c.  $\frac{1 + \log(7)}{2 + 3 \log(7)}$
- d.  $\frac{1}{1 + \log(7)}$
- e.  $1 + \log(7)$

15. Solve for  $t$  (time) in the following equation  $A = Pe^{-rt}$ .

- a.  $t = \frac{r}{\ln(A/P)}$
- b.  $t = \frac{\ln(P/A)}{r}$
- c.  $t = \frac{1 + \log(A)}{1 - \log(P)}$
- d.  $t = \frac{r \ln(A)}{P}$
- e.  $t = \frac{\ln(A/P)}{r}$

16. You want to invest \$5,000 to accumulate \$1,000,000 in 50 years. You decide to look for a bank that compounds the interest continuously. What annual interest rate should you look for? Approximate your answer to two decimal places.
- a. 10.60%
  - b. 11.51%
  - c. 13.82%
  - d. 8.83%
  - e. 7.57%
17. The area of a rectangle is given by the function  $A(x) = -x^2 + 6x + 20$ . Find the maximum value of its area.
- a. 47 square units
  - b. 29 square units
  - c. 7 square units
  - d. 90 square units
  - e. 15 square units
18. Only one of the following statements is true of the exponential function  $f(x) = e^x$ .
- a.  $y \rightarrow 0$  as  $x \rightarrow -\infty$  and  $y \rightarrow \infty$  as  $x \rightarrow \infty$
  - b.  $y \rightarrow \infty$  as  $x \rightarrow -\infty$  and  $y \rightarrow 0$  as  $x \rightarrow \infty$
  - c.  $y \rightarrow \infty$  as  $x \rightarrow -\infty$  and  $y \rightarrow \infty$  as  $x \rightarrow \infty$
  - d.  $y \rightarrow 0$  as  $x \rightarrow \infty$  and  $y \rightarrow -\infty$  as  $x \rightarrow -\infty$
  - e.  $y \rightarrow 0$  as  $x \rightarrow -\infty$  and  $y \rightarrow -\infty$  as  $x \rightarrow \infty$
19. What remainder do you get when you divide  $x^{89} - 2x^{50} + 1$  by  $x + 1$ ?
- a. 2
  - b. 4
  - c. -2
  - d. 3
  - e. 5
20. Solve the inequality  $\frac{x-8}{x+8} \geq 0$ .
- a.  $[-8, 8)$
  - b.  $(-\infty, -8) \cup [8, \infty)$
  - c.  $(-\infty, -8]$
  - d.  $[8, \infty)$
  - e.  $(-\infty, -8] \cup [8, \infty)$

21. Only one of the following statements is *true* for all values of  $x$  and  $y$ .

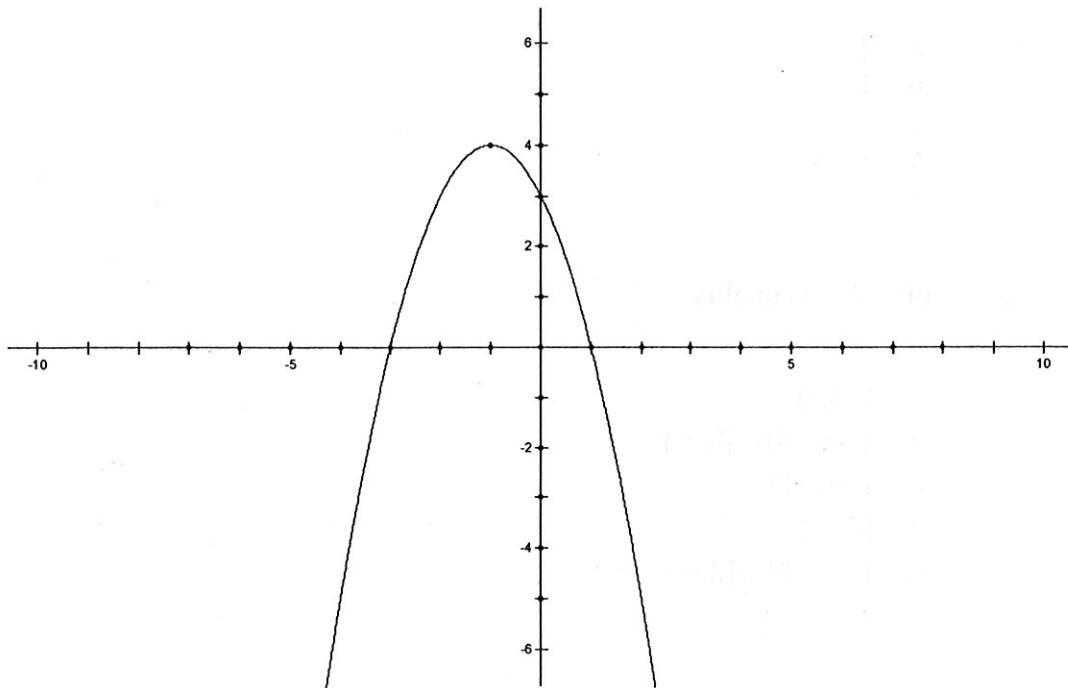
- a.  $\ln(x^3) = (\ln(x))^3$
- b.  $\ln\left(\frac{x}{y}\right) = \frac{\ln(x)}{\ln(y)}$
- c.  $\ln(e^{3x}) = 3x$
- d.  $\ln(x + y) = \ln(x) + \ln(y)$
- e.  $\log(x^3) = 3$

22. Solve for  $x$  in the following exponential equation,  $3^{x^2-3x-2} = \frac{1}{9}$ .

- a.  $x = -1$  or  $x = 4$
- b.  $x = 3$
- c.  $x = 0$  or  $x = 3$
- d.  $x = 0$
- e.  $x = 1$

23. Identify the solution set of the quadratic inequality  $-x^2 - 2x + 3 \leq 0$  by inspecting its graph.

- a.  $[-3, 1]$
- b.  $[-3, \infty)$
- c.  $(-\infty, 1]$
- d.  $[-3, 1]$
- e.  $(-\infty, -3] \cup [1, \infty)$



24. Axis of symmetry and vertex of the parabola  $f(x) = -x^2 - 2x + 3$  are

- a. Vertex =  $(-1, 4)$  and Axis of symmetry: line  $x = -1$
- b. Vertex =  $(-1, 4)$  and Axis of symmetry: line  $y = -1$
- c. Vertex =  $(-1, 4)$  and Axis of symmetry: line  $y = 4$
- d. Vertex =  $(-1, 4)$  and Axis of symmetry: line  $x = 1$
- e. Vertex =  $(4, -1)$  and Axis of symmetry: line  $x = -1$

25. If  $x = 2$  is a zero of  $f(x) = x^3 - 14x^2 + 59x - 70$ , find all the other zeros of  $f(x)$ .

- a.  $x = -7$  and  $x = -5$
- b.  $x = 7$  and  $x = -5$
- c.  $x = -7$  and  $x = 5$
- d.  $x = 7$  and  $x = 5$
- e. none of the above

26. The function  $f(x) = \frac{x^2}{x-1}$  is

- a. even
- b. odd
- c. neither even nor odd
- d. it is defined at 1
- e. defined for all real numbers

27. If  $f(x) = (x-1)^3$  and  $g(x) = \sqrt[3]{x} + 2$ ,  $(g \circ f)(x)$  is

- a.  $(g \circ f)(x) = (\sqrt[3]{x} + 1)^3$
- b.  $(g \circ f)(x) = x + 1$
- c.  $(g \circ f)(x) = x - 1$
- d.  $(g \circ f)(x) = \sqrt[3]{x} + 1$
- e.  $(g \circ f)(x) = (x-1)^2$

28. Give the algebraic expression for  $\cos(\sin^{-1}(x))$ . Here  $\sin^{-1}(x)$  stands for the compositional inverse of  $\sin(x)$ .

- a.  $\sqrt{1-x^2}$
- b.  $\sqrt{1+x^2}$
- c.  $\sqrt{x^2 - 1}$
- d.  $x^2 + 1$
- e.  $1 - x^2$

29. Which of the following expressions is equal to  $\cos(\alpha + \frac{\pi}{4})$ ? (Angles are measured in radians)

a.  $\frac{\sin(\alpha) + \cos(\alpha)}{\sqrt{2}}$

b.  $\frac{\sin(\alpha) - \cos(\alpha)}{\sqrt{2}}$

c.  $\frac{\cos(\alpha) - \sin(\alpha)}{\sqrt{2}}$

d.  $\frac{\sin(\alpha) - \cos(\alpha)}{2}$

e.  $\frac{\sin(\alpha) + \cos(\alpha)}{2}$

30. Determine the amplitude, period, and phase shift of  $f(x) = 4\sin(2x - 2\pi)$ .  
(Angles are measured in radians)

a. Amplitude: 2 and Period:  $2\pi$  and Phase shift:  $2\pi$

b. Amplitude: 4 and Period:  $\pi$  and Phase shift:  $\pi$

c. Amplitude: 2 and Period:  $\pi$  and Phase shift:  $2\pi$

d. Amplitude: 2 and Period: 2 and Phase shift:  $\pi$

e. Amplitude: 4 and Period:  $2\pi$  and Phase shift:  $2\pi$

31. Find the exact value of  $\cot(\sin^{-1}(\sqrt{2}/2))$ .

a.  $\pi/4$

b.  $-\pi/4$

c. 0

d. -1

e. 1

32.  $\sin 2k \cos k + \cos 2k \sin k$  is equal to

a.  $\cos 3k$

b.  $\cos k$

c.  $\sin k$

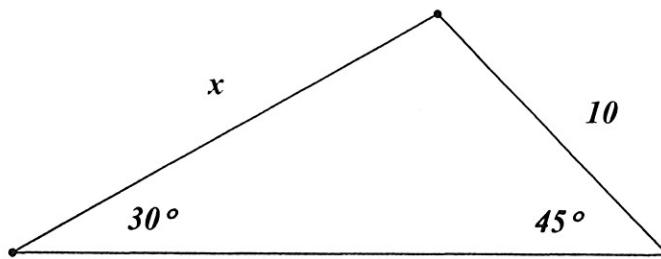
d.  $\sin 3k$

e.  $\cos 6k$

33. Find the general solution of the equation  $\cos(x) = \frac{1}{2}$ .

- a.  $x = \frac{\pi}{3} + k2\pi$
- b.  $x = \frac{5\pi}{3} + k2\pi$
- c.  $x = \frac{\pi}{3} + k2\pi, x = \frac{5\pi}{3} + k2\pi$
- d.  $x = \frac{\pi}{6} + k2\pi, x = \frac{11\pi}{6} + k2\pi$
- e.  $x = \frac{\pi}{3} + k\pi, x = \frac{5\pi}{3} + k\pi$

34. Find the value of  $x$  in the following triangle. Round your answer to two decimal places.



- a.  $10\sqrt{2}$
- b.  $5\sqrt{2}$
- c.  $5/\sqrt{2}$
- d.  $10/\sqrt{2}$
- e.  $\sqrt{2}/10$

35. Use the trigonometric identities to simplify the expression  $\frac{1 - \cos(2\theta)}{1 + \cos(2\theta)}$

- a.  $\tan^2(\theta)$
- b.  $\frac{2\sin(\theta)}{\cos(\theta)}$
- c.  $\frac{1 - \cos(\theta)}{1 + \cos(\theta)}$
- d. 1
- e.  $\tan(\theta)$